

# SPATIO-TEMPORAL METHODOLOGY TO ASSESS AND COMPARE THE DIFFERENCES OF LONGEVITY IN EUROPE.

**P.Carracedo**<sup>1,2</sup> A. Debón<sup>1</sup>

<sup>1</sup>Centro de gestión de la Calidad y del Cambio  
Universitat Politècnica de València (Spain)

**e-mail:patcarga@posgrado.upv.es**

<sup>2</sup>Valencian International University (Spain)

June 30, 2016, Valencia.

## Main objective

In this study, there are **two objectives**:

- The first one is to present **a spatial-temporal methodology to test significant clusters (groups)** of 26 European countries over a period of 20 years with different behaviour.
- The second is to study the space-time dependence of significant clusters through a **spatial panel data model**.

## Motivation

In general, all the countries of the European Union have suffered a decrease in mortality during the last century, but nevertheless **the gap between the mortality of Eastern and Western Europe countries is growing** (Leon, 2011; Vaupel et al., 2011).

## Data

- This study is based on mortality data from **26 European countries** for the **period 1990-2009** and **an age range from zero to +110**.
- These data were obtained from the database *HMD (2014)* for a total of 26 European countries: Austria, Belarus, Belgium, Czech Republic, Denmark, Estonia, Finland, France, Germany, Hungary, Ireland, Italy, Latvia, Lithuania, Luxembourg, Netherlands, Norway, Poland, Portugal, Slovakia, Slovenia, Spain, Sweden, Switzerland, UK and Ukraine.
- In addition, for these 26 countries and 20 years, we collect information of seven covariates: ***Gross Domestic Product (GDP)***, ***Activity rate***, ***Energy consumption and Birth rate***, from the database *The World Bank (2015)*.

## Statistics

To study the spatio-temporal relationship of mortality in European countries, several statistics have been used:

- Standardised Mortality Ratio (SMR)
- Global Moran Index
- Local Moran Index
- Spatial Markov

## Selected model

The typology of our data leads us to use a **Fixed Effects Spatial Lag Model**. The reasons are:

- **Fixed Effects:** The fixed effects model is generally more appropriate than the random effects model since spatial econometricians tend to work with space-time data of adjacent spatial units located in unbroken study areas (Elhorst, 2014).
- **Spatial Lag:** We confirm that the value of the SMR in a country depends on the value of SMR in another country adjacent.

## Mathematical formula

The **Fixed Effects Spatial Lag Model** is expressed as follows:

$$y_{it} = \lambda \sum_{j=1}^N W_{ij} y_{jt} + X_{it} \beta + \mu_i + \nu_t + \epsilon_{it}$$

where:

$i$  represents the countries

$t$  represents the years

$y_{it}$  is an observation on the dependent variable at  $i$  and  $t$

$\lambda$  is the spatial parameter associated with the dependent variable

$W_{ij}$  spatial weights matrix where  $i$  and  $j$  represent whichever two of the  $N$  countries

$x_{it}$  vector of observations on the independent variables

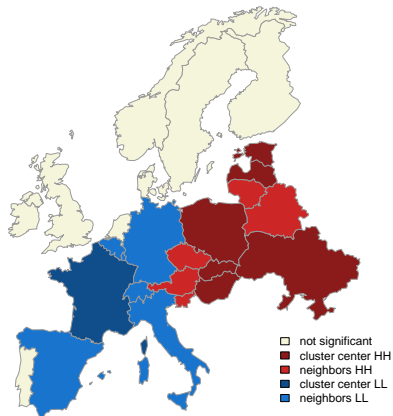
$\beta$  vector of fixed but unknown parameters

$\mu_s$  is the spatial fixed effect (not spatially autocorrelated)

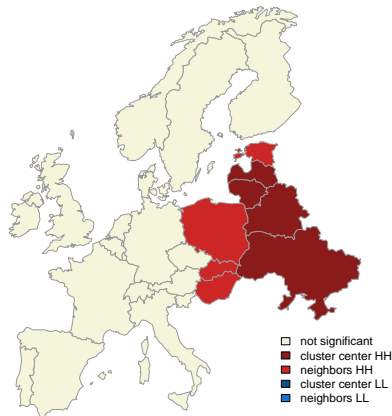
$\nu_t$  is the temporal fixed effect (not temporal autocorrelation)

$\epsilon_{it}$  is the error model (not spatially autocorrelated)

## Clusters Map for years 1990 and 2009 in Europe.



(a) Cluster Map Europe in 1990



(b) Cluster Map Europe in 2009

# Parameter estimation of Fixed Effects Spatial Lag Model

```
> f <- (logSMR ~ GDP + activity rate + energy consumption)
> model3cov<- spml(f,data,index=c("country","year"), listw = pesosmatl
w,lag=TRUE,model = "within", spatial.error="none", effect="twoways")
>
> summary(model3cov)
Spatial panel fixed effects lag model
```

```
Call:
spml(formula = f, data = data_imp2, index = c("country", "year"),
      listw = pesosmatlw, model = "within", effect = "twoways",
      lag = TRUE, spatial.error = "none")
```

Residuals:

Min.	1st Qu.	Median	3rd Qu.	Max.
-0.216000	-0.018900	-0.000858	0.018000	0.143000

Coefficients:

	Estimate	Std. Error	t-value	Pr(> t )	
lambda	0.34646104	0.03909351	8.8624	< 2.2e-16	***
GDP	0.00411959	0.00059531	6.9201	4.514e-12	***
activity rate	-0.00329698	0.00087190	-3.7814	0.000156	***
energy consumption	-0.00405517	0.00076275	-5.3165	1.058e-07	***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1



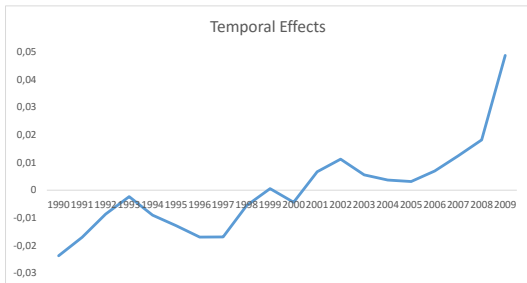
# Parameter estimation of Fixed Effects Spatial Lag Model cont...

```
> effects(model3cov)

Intercept:
      Estimate Std. Error t-value Pr(>|t|)
(Intercept) 0.289611  0.052336  5.5337 3.135e-08 ***

Spatial fixed effects:
      Estimate Std. Error t-value Pr(>|t|)
austria    -0.1367964  0.0533695 -2.5632  0.010371 *
belgium     -0.1182289  0.0462476 -2.5564  0.010575 *
belarus     0.2724464  0.0529076  5.1495 2.612e-07 ***
switzerland -0.1821221  0.0607600 -2.9974  0.002723 **
czech.republic 0.1167373  0.0531932  2.1946  0.028193 *
germany     -0.1025211  0.0522681 -1.9614  0.049827 *
denmark     0.0348714  0.0592428  0.5886  0.556117
estonia     0.1350265  0.0550526  2.4527  0.014180 *
spain       -0.1977822  0.0496440 -3.9840 6.776e-05 ***
finland     -0.0673335  0.0544749 -1.2360  0.216441
france      -0.2255814  0.0499580 -4.5154 6.319e-06 ***
hungary     0.2043721  0.0450712  4.5344 5.776e-06 ***
ireland     -0.0074169  0.0540874 -0.1371  0.890930
italy       -0.2122881  0.0452491 -4.6915 2.712e-06 ***
lithuania   0.1160925  0.0543955  2.1342  0.032824 *
luxembourg  0.0224167  0.0564338  0.3972  0.691204
latvia      0.2544437  0.0545260  4.6665 3.064e-06 ***
netherlands -0.1217289  0.0550242 -2.2123  0.026947 *
norway      -0.1231497  0.0574568 -2.1433  0.032085 *
poland      0.0522064  0.0511289  1.0211  0.307219
portugal    0.0381412  0.0553676  0.6889  0.490903
sweden      -0.1727348  0.0563408 -3.0659  0.002170 **
slovenia    0.0213348  0.0527795  0.4042  0.686047
slovakia    0.1270905  0.0540766  2.3502  0.018764 *
ukraine     0.3611898  0.0512787  7.0437 1.873e-12 ***
uk          -0.0886855  0.0556644 -1.5932  0.111111
```

## Graphical representation of temporal effect



## Acknowledgements

This work was supported by grant from *Ministerio de Economía y Competitividad (MTM2013-45381)*.

*Thanks for your attention*  
Any question?

Patricia Carracedo  
Centro de gestión de la Calidad y del Cambio  
Universitat Politècnica de València (Spain)  
e-mail: [patcarga@posgrado.upv.es](mailto:patcarga@posgrado.upv.es)

- Bivand, R. (2014). *spdep: Spatial dependence: weighting schemes, statistics and models. R package, version 0.5-77.*  
<http://CRAN.R-project.org/package=spdep>.
- Bivand, R. and Lewin-Koh, N. (2014). *maptools: Tools for reading and handling spatial objects. R package version 0.8-29.*  
<http://CRAN.R-project.org/package=maptools>.
- Croissant, Y. and Millo, G. (2008). Panel data econometrics in R: The plm package. *Journal of Statistical Software*, 27(2).
- Elhorst, J. P. (2014). Spatial panel data models. In *Spatial Econometrics*, pages 37–93. Springer.
- HMD (2014). Human Mortality Database. University of California, Berkeley (USA), and Max Planck Institute for Demographic Research (Germany). Available at [www.mortality.org](http://www.mortality.org) or [www.humanmortality.de](http://www.humanmortality.de) (data downloaded 17th April 2014).
- Hyndman, R. J., Booth, H., Tickle, L., and Maindonald, J. (2014). *demography: Forecasting mortality, fertility, migration and population data.*

- Laurent, T., R.-G. A. and Thomas-Agnan, C. (2012). Geoxp: An r package for exploratory spatial data analysis. *Journal of Statistical Software*, 47(2):1–23. URL <http://www.jstatsoft.org/v47/i02/>.
- Leon, D. A. (2011). Trends in European life expectancy: a salutary view. *International Journal of Epidemiology*.
- Millo, G. and Piras, G. (2012). splm: Spatial panel data models in R. *Journal of Statistical Software*, 47(1):1–38.
- The World Bank (2015). World Bank Open Data: free and open access to data about development in countries around the globe. <http://data.worldbank.org/>. [consultada en enero 2015].
- Vaupel, J. W., Zhang, Z., and van Raalte, A. A. (2011). Life expectancy and disparity: an international comparison of life table data. *BMJ open*, 1(1).